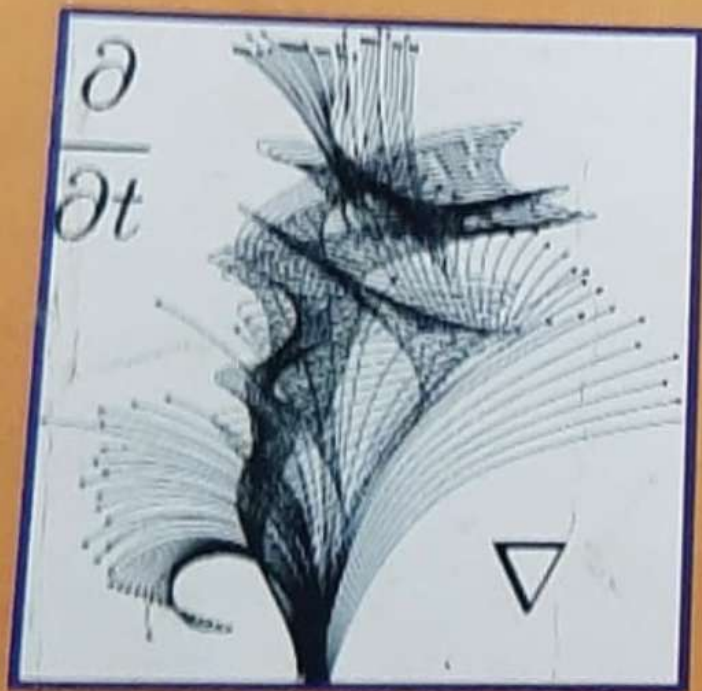


PARTIAL DIFFERENTIAL EQUATIONS

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A Sister Concern of Pragati Prakashan



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PARTIAL DIFFERENTIAL EQUATIONS

For B.A./B.Sc. II Year (Third Semester) Students of M.D.U., K.U. & C.D.L.U.

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Examination Papers