KU

BUSINESS MATHEMATICS

Vol. I

VIJAY CHAWLA • SANJAY GARG • JATINDER KAUR • UPASNA • SAURABH SINGLA

A. S. PRAKASHAN, MEERUT

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BUSINESS MATHEMATICS

For B.Com. 1 Year (First Semester) Students of K.U. Kurukshetra

As per new syllabus 2017-18

B.Com IST General
Roll No. - 1813014

Dr. VIJAY CHAWLA
Assistant Professor
Head, Department of Mathematics
Maharaja Agrasen College,
Jagadhri YAMUNANAGAR

Dr. SANJAY GARG
Assistant Professor
Department of Mathematics
R. K. S. D. (PG) College,
KAITHAL

Dr. JATINDER KAUR
Associate Professor
Department of Mathematics
Guru Nanak Girls College,
YAMUNANAGAR

Dr. UPASNA
Associate Professor
Department of Mathematics
Dayanand Mahila Mahavidalya,
KURUKSHETRA

SAURABH SINGLA
Assistant Professor
Department of Mathematics
I.G.N. College,
LADWA

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A. S. PRAKASHAN
D-106, Saket, Meerut 250 001, U.P.
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A.S. PRAKASHAN
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D-106, Saket, Meerut
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e-mail : asprakashanmrt@gmail.com

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Syllabus

BUSINESS MATHEMATICS-I
(BC-105)

Time: 3 Hours

External Marks: 80
Internal Marks: 20

Note : Paper setter will set nine questions in all. Question No. 1 comprising of five short types questions carrying four (4) marks each is compulsory. It covers the entire syllabus. Answer to each question should not be more than one page. Candidate is required to attempt four questions from the remaining eight questions carrying 15 marks each.

Logarithms, Anti-logarithms

Sequences and Series : Arithmetic & Geometric Progressions.

Differentiation : Idea of simple derivative of different functions (excluding Trigonometrical functions); Rules of differentiation (simple standard forms).

Maxima and Minima of functions of one variable (including 2nd or 3rd order derivatives) relating to cost, revenue and profit.

Matrices and Determinants : concept of matrix, types, and algebra of matrices; properties of determinants; calculation of values of determinants up to third order, adjoint of a matrix, elementary row or column operations; Finding inverse of a matrix through adjoint and elementary row or column operations; solution of a system of linear equations having unique solution and involving not more than three variables.

Compound Interest and Annuities : different types of interest rates, concept of present value and amount of a sum; types of annuities; present value and amount of an annuity (including the case of continuous compounding); valuation of simple loans and debentures; problems relating to sinking funds.

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